

2) a) Confirm $\int x \sin x dx = \sin x - x \cos x + C$

$$\frac{d}{dx} (\sin x - x \cos x + C) = \frac{d}{dx} (\overset{1}{\sin x}) - \frac{d}{dx} (\overset{2}{x \cos x}) + \frac{d}{dx} (\overset{3}{C})$$

$$= \overset{1}{\cos x} - \left[(\overset{2}{1}) \cos x + x (-\overset{2}{\sin x}) \right] + 0$$

$$= \cos x - \cos x + x \sin x$$

$$= x \sin x$$

b) Confirm: $\int \frac{dx}{(1-x^2)^{3/2}} = \frac{x}{\sqrt{1-x^2}} + C$

#3256
Q9

3) find a deriv & state an integration rule

$$\frac{d}{dx} [\sqrt{x^3+5}] = \frac{d}{dx} (x^3+5)^{1/2}$$

$$= \frac{1}{2} (x^3+5)^{-1/2} (3x^2)$$

$$= \frac{3}{2} \frac{x^2}{\sqrt{x^3+5}}$$

$$\int \frac{3}{2} \frac{x^2}{\sqrt{x^3+5}} dx = \sqrt{x^3+5} + C$$

$$\underline{5)} \quad \frac{d}{dx} \sin(2\sqrt{x}) = \cos(2\sqrt{x}) \frac{d}{dx}(2\sqrt{x}) \quad 2x^{1/2}$$

$$= \cos(2\sqrt{x}) (x^{-1/2})$$

$$= \frac{\cos(2\sqrt{x})}{\sqrt{x}}$$

$$\int \frac{\cos(2\sqrt{x})}{\sqrt{x}} dx = \sin(2\sqrt{x}) + C$$

$$4) \quad \frac{d}{dx} \left(\frac{x}{x^2+3} \right) = \frac{(1)(x^2+3) - (x)(2x)}{(x^2+3)^2} = \frac{3-x^2}{(x^2+3)^2}$$

12	15
4	17
8	10

$$\int \frac{(x^2+3) - (x)(2x)}{(x^2+3)^2} dx = \frac{x}{x^2+3} + C$$

$$\int \frac{3-x^2}{(x^2+3)^2} dx = \frac{x}{x^2+3} + C$$

$$\begin{array}{l}
 \underline{8)} \int \sqrt[3]{x^2} dx \\
 = \int x^{2/3} dx \\
 = \frac{x^{5/3}}{5/3} + C \\
 = \frac{3x^{5/3}}{5} + C \\
 = \frac{3\sqrt[3]{x^5}}{5} + C
 \end{array}
 \left.
 \begin{array}{l}
 \int \frac{1}{x^6} dx \\
 \int x^{-6} dx \\
 = \frac{x^{-5}}{-5} + C \\
 = \frac{-1}{5x^5} + C
 \end{array}
 \right\}
 \begin{array}{l}
 \int x^{-7/8} dx \\
 = \frac{x^{1/8}}{1/8} + C \\
 = 8x^{1/8} + C \\
 = 8\sqrt[8]{x} + C
 \end{array}$$

$$10) \int x^{2/3} - 4x^{-1/5} + 4 \, dx \quad 12) \int \frac{7}{y^{3/4}} - \sqrt[3]{y} + 4\sqrt{y} \, dy$$

$$= \int x^{2/3} dx - 4 \int x^{-1/5} dx + \int 4 dx = \int 7y^{-3/4} - y^{1/3} + 4y^{1/2} dy$$

$$= \frac{x^{5/3}}{5/3} - 4 \left(\frac{x^{4/5}}{4/5} \right) + 4x + C = \frac{y^{1/4}}{1/4} - \frac{y^{4/3}}{4/3} + 4 \left(\frac{y^{3/2}}{3/2} \right) + C$$

$$\int 4 dx = \int 4x^0 dx = 4 \frac{x^1}{1} = 4x + C = 28y^{1/4} - 3\frac{y^{4/3}}{4} + \frac{8y^{3/2}}{3} + C$$

$$\underline{15)} \int x^{1/3} (2-x)^2 dx = \int x^{1/3} (4 - 4x + x^2) dx$$

$$= \int 4x^{1/3} - 4x^{4/3} + x^{7/3} dx$$

$$= 4 \frac{x^{4/3}}{4/3} - 4 \frac{x^{7/3}}{7/3} + \frac{x^{10/3}}{10/3} + C$$

$$= 3x^{4/3} - \frac{12x^{7/3}}{7} + \frac{3x^{10/3}}{10} + C$$

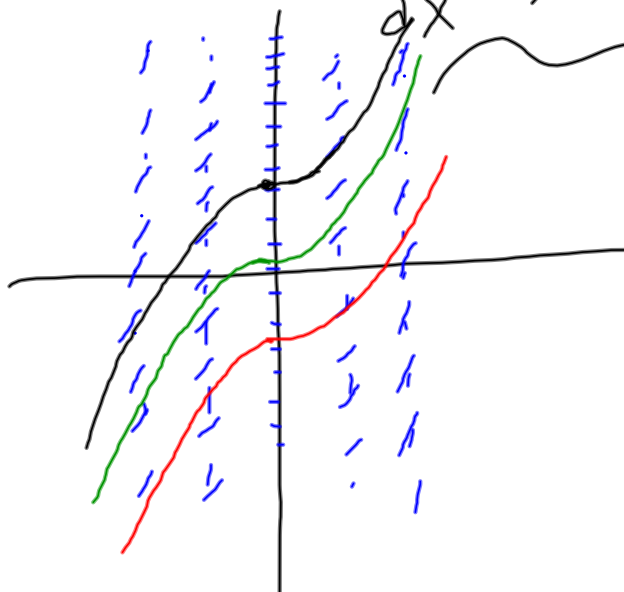
$$(17) \int \frac{x^5 + 2x^2 - 1}{x^4} dx = \int \frac{x^5}{x^4} + \frac{2x^2}{x^4} - \frac{1}{x^4} dx$$

$$= \int x + 2x^{-2} - x^{-4} dx$$

$$= \frac{x^2}{2} - \frac{2x^{-1}}{-1} - \frac{x^{-3}}{-3} + C$$

41 pre-A

$$\frac{dy}{dx} = x^2 ; y(0) = 3$$



x	$\frac{dy}{dx} = x^2$
0	0
1	1
-1	1
2	4

$$\frac{dy}{dx} = x^2$$

$$y = \frac{x^3}{3} + C$$

$$3 = \frac{0^3}{3} + C$$

$$3 = C$$

$$y = \frac{x^3}{3} + 3$$

41a) $\frac{dy}{dx} = \sqrt[3]{x} ; y(1)=2$

Find antiderivative $\left(\frac{dy}{dx}\right) = (x^{1/3})$ Find antiderivative

$$y = \frac{x^{4/3}}{4/3} + C$$

$$y = \frac{3\sqrt[3]{x^4}}{4} + C$$

$y=2$ when $x=1$

$$2 = \frac{3\sqrt[3]{1^4}}{4} + C$$

$$2 = \frac{3}{4} + C ; C = \frac{5}{4}$$

$$\therefore y = \frac{3}{4}\sqrt[3]{x^4} + \frac{5}{4}$$

41b) $\frac{dy}{dx} = \sin t + 1$; $y\left(\frac{\pi}{3}\right) = \frac{1}{2}$

Find derivative
of $\frac{dy}{dx} = \sin t + 1$

$y = -\cos t + t + C$
when $x = \frac{\pi}{3}$ and $y = \frac{1}{2}$

$\frac{1}{2} = -\cos\left(\frac{\pi}{3}\right) + \frac{\pi}{3} + C$

$\frac{1}{2} = -\frac{1}{2} + \frac{\pi}{3} + C$

$\left(1 - \frac{\pi}{3}\right) = C$

$F'(x) = f(x)$

$\int f(x) dx = ? F(x)$

$y = -\cos t + t + \left(1 - \frac{\pi}{3}\right)$

41c) $\frac{dy}{dx} = \frac{x+1}{\sqrt{x}}; y(1)=0$ ($\frac{x^0}{x^{1/2}} = \frac{1}{x^{1/2}} = x^{-1/2}$)

$$\frac{dy}{dx} = \frac{x+1}{\sqrt{x}} = \frac{x}{\sqrt{x}} + \frac{1}{\sqrt{x}} = \frac{x^1}{x^{1/2}} + \frac{1}{x^{1/2}} = x^{1/2} + x^{-1/2}$$

$$\int \frac{dy}{dx} dx = \int x^{1/2} + x^{-1/2} dx$$

$$y = \frac{2x^{3/2}}{3} + \frac{2x^{1/2}}{1} + C = \frac{2x^{3/2}}{3} + 2\sqrt{x} + C$$

when $x=1, y=0$

$$0 = \frac{2}{3}(1) + 2(1) + C$$

$$-\frac{8}{3} = -\frac{2}{3} - 2 \Rightarrow \textcircled{1}$$

$$y = \frac{2}{3}x^{3/2} + 2\sqrt{x} - \frac{8}{3}$$

39) a point moves along a curve $y = f(x)$
so that at each pt (x, y) on the curve, the slope
of the tangent line is $-\sin x$.

Find an equation for the curve given $(0, 2)$ is
on curve.

$$\frac{dy}{dx} = -\sin x \Rightarrow y = \cos x + C$$

$$2 = \cos(0) + C$$

$$2 = 1 + C \Rightarrow C = 1$$

$$y = \cos x + 1$$

6.2 Homework

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$$a) \frac{dy}{dx} = \frac{1}{(2x)^3}; y(1) = 0$$

$$\begin{aligned} u &= 2x \\ du &= 2dx \\ \frac{1}{2} du &= dx \\ \frac{1}{2} \int u^{-3} du \\ \frac{1}{2} \cdot \frac{u^{-2}}{-2} + C \\ &= -\frac{1}{4(2x)^2} + C \end{aligned}$$

$$\int \frac{1}{8x^3} dx = \frac{1}{8} \int x^{-3} dx$$

$$= \frac{1}{8} \frac{x^{-2}}{-2} + C = -\frac{1}{16x^2} + C$$

$$y = -\frac{1}{16x^2} + C$$

$$y(1) = 0$$

$$0 = -\frac{1}{16(1)^2} + C$$

$$\therefore C = \frac{1}{16}$$

$$y = -\frac{1}{16x^2} + \frac{1}{16}$$

$$b) \frac{dy}{dx} = \sec^2(t) - \sin(t); y\left(\frac{\pi}{4}\right) = 1$$

$$\int \sec^2(t) dt - \int \sin(t) dt$$

$$\tan(t) - (-\cos(t)) + C$$

$$y = \tan(t) + \cos(t) + C$$

$$y\left(\frac{\pi}{4}\right) = 1$$

$$1 = \tan\left(\frac{\pi}{4}\right) + \cos\left(\frac{\pi}{4}\right) + C$$

$$1 = 1 + \frac{\sqrt{2}}{2} + C$$

$$\therefore C = -\frac{\sqrt{2}}{2}$$

$$y = \tan(t) + \cos(t) - \frac{\sqrt{2}}{2}$$

2) confirm $\int x \sin x \, dx = \sin x - x \cos x + C$


$$\frac{d}{dx} (\sin x) - \frac{d}{dx} (x \cos x) + \frac{d}{dx} (C)$$

$$= \cos x - [(1) \cos x + x(-\sin x)] + 0$$

$$= \cos x - \cos x + x \sin x$$

$$= \underline{x \sin x} \quad \checkmark$$

7c 8c
9 2
11



$$\frac{d}{dx} (1-x^2)^{1/2} =$$

$$\frac{1}{2} (1-x^2)^{-1/2} \frac{d}{dx} (1-x^2)$$

2b) $\int \frac{1}{(1-x^2)^{3/2}} \, dx = \frac{x}{(1-x^2)^{1/2}} + C$

$$\frac{d}{dx} \left(\frac{x}{(1-x^2)^{1/2}} \right) = \frac{(1)(1-x^2)^{1/2} - x \left(\frac{1}{2} (1-x^2)^{-1/2} (-2x) \right)}{\left((1-x^2)^{1/2} \right)^2}$$

$$= \frac{\left(\frac{\sqrt{1-x^2}}{\sqrt{1-x^2}} \right) + \frac{x^2}{\sqrt{1-x^2}}}{(1-x^2)} = \frac{(1-x^2) + x^2}{(1-x^2)^{3/2}}$$

$\sqrt{1-x^2} \cdot \sqrt{1-x^2} = (\sqrt{1-x^2})^2$

$$\frac{\frac{a}{b} \left(\frac{1}{c} \right)}{c \left(\frac{1}{c} \right)} = \frac{a}{bc}$$

$$= \frac{1}{\frac{\sqrt{1-x^2}}{(1-x^2)}} = \frac{1}{(1-x^2)^{3/2}}$$

$$7c) \int x^3 \sqrt{x} dx =$$

$$\int (x^3)(x^{1/2}) dx = \int x^{7/2} dx$$

$$= \frac{x^{9/2}}{\frac{9}{2}} + C = \frac{2}{9} x^{9/2} + C$$

$$8c) \int x^{-7/8} dx = \frac{x^{1/8}}{\frac{1}{8}} + C = 8x^{1/8} + C$$



$$\begin{aligned}
 9) \quad & \int \frac{1}{2x^3} dx \\
 &= \frac{1}{2} \int \frac{1}{x^3} dx \\
 &= \frac{1}{2} \int x^{-3} dx \\
 &\quad \quad \quad -3+1 = -2 \\
 &= \left(\frac{1}{2}\right) \left(\frac{x^{-2}}{-2}\right) + C \\
 &= -\frac{1}{4x^2} + C
 \end{aligned}$$

$$\begin{aligned}
 & \int u^3 - 2u + 7 \, du \\
 &= \left(\int u^3 du\right) - 2\left(\int u du\right) + 7\left(\int 1 du\right) \quad \text{find} \\
 &= \frac{u^4}{4} - 2\left(\frac{u^2}{2}\right) + 7(u) + C \\
 &= \frac{u^4}{4} - u^2 + 7u + C \\
 &\sqrt{\frac{d}{dx} \left(\frac{u^4}{4} \right) = \frac{1}{4} \frac{d}{dx} (u^4) = \frac{1}{4} (4u^3)}
 \end{aligned}$$

$$\underline{11)} \int x^{-3} + \sqrt{x} - 3x^{1/4} + x^2 dx$$

$$= \int x^{-3} dx + \int x^{1/2} dx - 3 \int x^{1/4} dx + \int x^2 dx$$

$$= \frac{x^{-2}}{-2} + \frac{x^{3/2}}{3/2} - 3 \left(\frac{x^{5/4}}{5/4} \right) + \frac{x^3}{3} + C$$

$$= -\frac{1}{2x^2} + \frac{2x^{3/2}}{3} - \frac{12x^{5/4}}{5} + \frac{x^3}{3} + C$$



6.2 Homework

$$8) \int \sqrt[3]{x^2} dx$$

WB

$$\frac{d}{dx}(e^x) = e^x$$

$$\frac{d}{dx}(\ln x) = \frac{1}{x}$$

$$= \int x^{2/3} dx$$

$$= \frac{x^{5/3}}{5/3} + C$$

$$= \frac{3x^{5/3}}{5} + C$$

$$\int \frac{1}{x^6} dx$$

$$\int x^{-6} dx$$

$$= \frac{x^{-5}}{-5} + C$$

$$= -\frac{1}{5x^5} + C$$

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$$\int x^{-7/8} dx$$



21

$$\underline{21)} \int 4\sin x + 2\cos x dx$$
$$= 4 \int \sin x dx + 2 \int \cos x dx$$

$$= 4(-\cos x) + 2(\sin x) + C$$

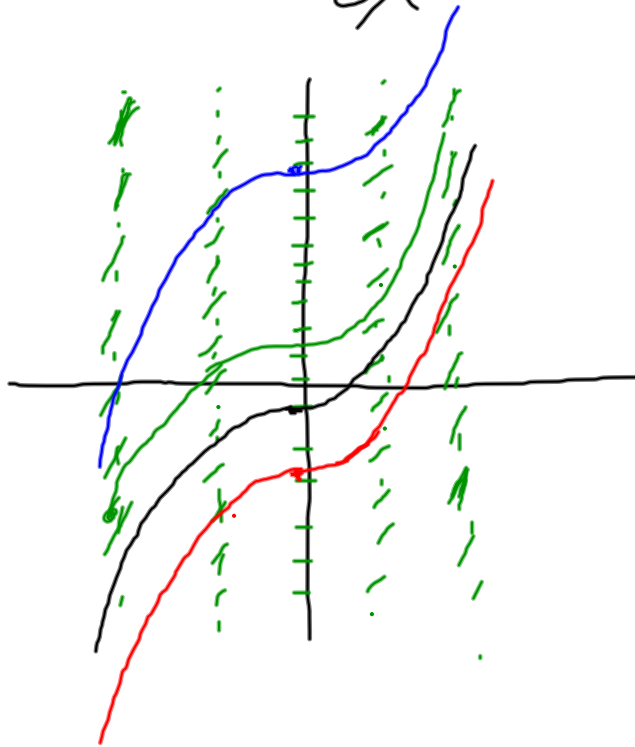
$$= -4\cos x + 2\sin x + C$$



$$\frac{7}{y^{3/4}} = 7y^{-3/4}$$

pre 41)

$$\frac{dy}{dx} = x^2; \quad y(0) = 3$$



x	$\frac{dy}{dx} = x^2$
0	0
-1	1
1	1
2	4
-2	4

Find $\frac{dy}{dx}$ = Find (x^2)

$$y = \frac{1}{3}x^3 + C$$

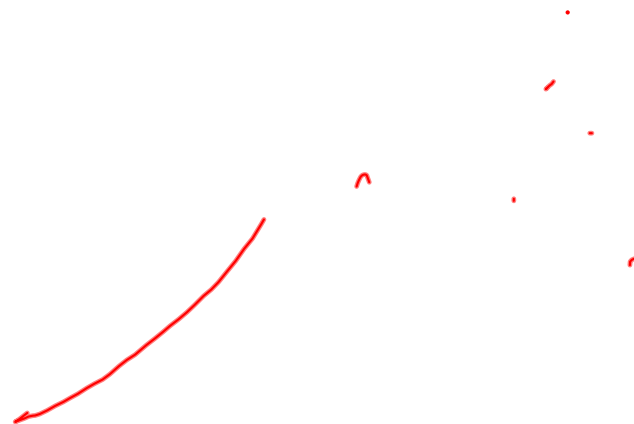
when $x=0, y=3$

$$3 = \frac{1}{3}(0)^3 + C$$

$$3 = 0 + C$$

$$C = 3$$

$$y = \frac{1}{3}x^3 + 3$$



41b $\frac{dy}{dx} = \sin t + 1$; $y(\frac{\pi}{3}) = \frac{1}{2}$

$$y = -\cos t + t + C$$

$$\frac{1}{2} = -\cos\left(\frac{\pi}{3}\right) + \frac{\pi}{3} + C$$

$$\frac{1}{2} = -\frac{1}{2} + \frac{\pi}{3} + C$$

$$1 - \frac{\pi}{3} = C$$

$$y = -\cos t + t + \left(1 - \frac{\pi}{3}\right)$$

4739
45
41b



$$\frac{d}{dx}(?)$$

$$= \sin x$$

$$\frac{d}{dx}(?)$$

$$= 1$$

39) Suppose a pt moves along a curve

⇒ at (x, y) the slope of the tangent line = $-\sin x$.



Find an eqⁿ for the curve given it skews $(0, 2)$

$$\frac{dy}{dx} = -\sin x \Rightarrow y = \cos x + C$$

$$2 = \cos 0 + C$$

$$2 = 1 + C$$

$$1 = C$$

$$y = \cos x + 1$$

45) Find general form of a function
whose 2ND deriv = \sqrt{x}



$$\sqrt{x} = x^{1/2} \quad \int x^{1/2} = \frac{2}{3} x^{3/2} + C_1$$

$$\frac{2}{3} x^{3/2} \quad \int \frac{2}{3} x^{3/2} = \frac{2}{3} \left(\frac{2}{5} x^{5/2} \right) + C_1 x + C_2 \quad \boxed{\frac{2}{3} \times \frac{2}{5} = \frac{4}{15}}$$

$$\frac{4}{15} x^{5/2} + C_1 x + C_2$$

$$\int x + x^2 + x^3 dx =$$

47) At each pt (x, y) on the curve
the slope is $2x+1$; $(-3, 0)$



$$\frac{dy}{dx} = 2x+1$$

$$y = x^2 + x + C \rightarrow y = x^2 + x - 6$$

$$0 = (-3)^2 + (-3) + C$$

$$0 = 9 - 3 + C$$

$$C = -6$$

6.2 Homework

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